

## **AME 486 Bonus Project**

**[Replace Final]**

Henry Glover

- **Cylinder modelling**
  - Height = 50in
  - Radius = 30in
- **Access hole**
  - Diameter = 10in
  - Distance of center from end = 25in
    - Hole is in the middle of the cylinder
- **Shell material**
  - Laminate = [0 /+30/-30/45/-45/+30/-30/0]
  - Ply thickness = 0.008 in
  - 0 degrees = parallel to cylinder axis
  - Physical properties
    - E11 = 12Msi = 12 e6 psi
    - E22 = 12Msi = 12 e6 psi
    - V12 = 0.05
    - G12 = 0.7Msi = 0.7 e6 psi
    - G13 = 0.5Msi = 0.5 e6 psi
    - G23 = 0.5Msi = 0.5 e6 psi
- **Modelling setup**
  - Element = S4
- **Boundary condition**
  - Clamped-clamped, allow movement in cylinder axial direction on one end
  - Characterized by 2 BCs
    - BC1: pin one end edge of cylinder
    - BC2: other end edge of the cylinder is only allowed movement in cylinder axis direction (z-direction)
- **Unit definition**
  - Length as inch
  - Mass as lb.
  - Time as seconds
- **Derived units**
  - Pressure as psi
  - Load as lb.

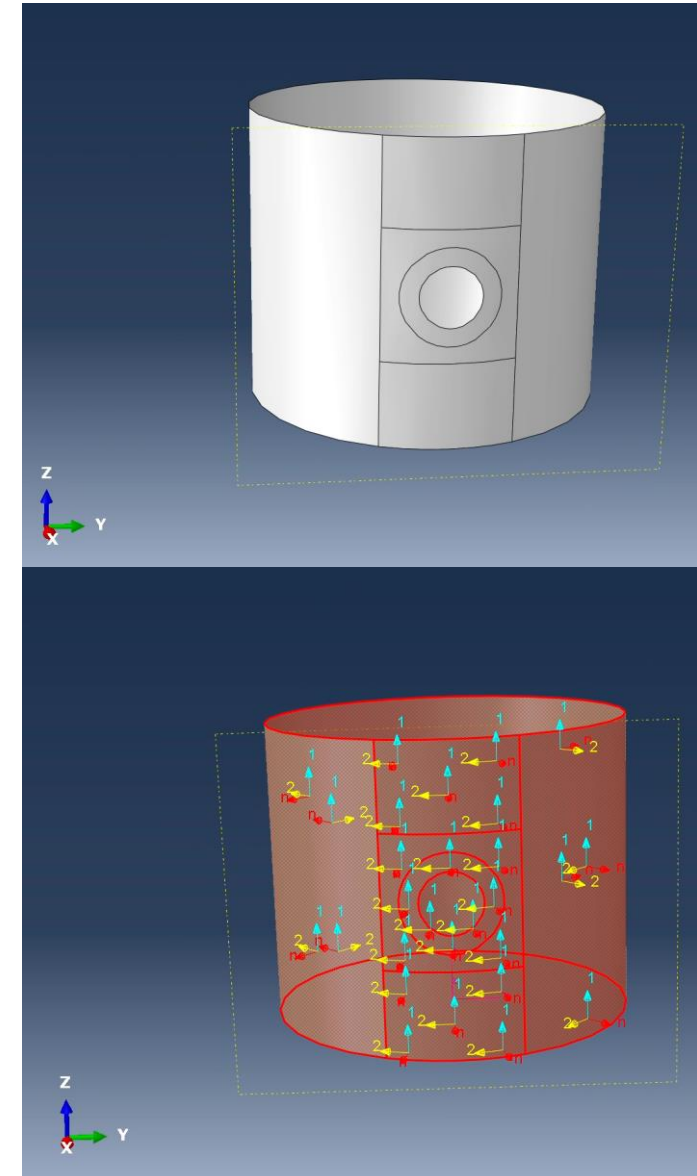
<https://www.youtube.com/watch?v=Ko8CfcbyDq0&t=1188s>

- **Model construction**

- 3D shell using extrusion
- Datum plane on selected principal plane
- Cut extrude set to go through one side of cylinder
- Partitioned one side of the cylinder with hole to refine mesh control in that region
  - Leads to better results

- **Composite ply angle global orientation**

- The ply rotation angle is defined relative to the reference axis (ref1)
- Ref1 needs to align along the cylinder's axis to correctly define fiber orientations
- To fix the misalignment
  - The normal axis needed to be adjusted
  - Axis 1 was set parallel to the cylinder's length
  - We see this in the bottom image to the right, where the blue arrow is pointing up



- Material properties
  - Mechanical – Elastic – Lamina properties set
  - Based on given values from the problem statement
- Composite ply angle's
  - 0-deg ply is along the axis of the cylinder
  - 8 total ply's, **NOT SYMMETRIC**
  - Material orientation was assigned to the cylinder
  - Assign composite layup so I don't need to spend extra computing time on calculating over every single ply

Edit Section

Name: CFRP\_Sec

Type: Shell / Continuum Shell, Composite

Section integration:
 ☒ During analysis
 ☐ Before analysis

Layup name:

Basic

Advanced

Thickness integration rule:
 ☒ Simpson
 ☐ Gauss

☐ Symmetric layers

| Material | Thickness | Orientation Angle | Integration Points | Ply Name |
|----------|-----------|-------------------|--------------------|----------|
| CRFP     | 0.008     | 0                 | 3                  |          |
| CRFP     | 0.008     | 30                | 3                  |          |
| CRFP     | 0.008     | -30               | 3                  |          |
| CRFP     | 0.008     | 45                | 3                  |          |
| CRFP     | 0.008     | -45               | 3                  |          |
| CRFP     | 0.008     | 30                | 3                  |          |
| CRFP     | 0.008     | -30               | 3                  |          |
| CRFP     | 0.008     | 0                 | 3                  |          |

Options:

OK

Cancel

Edit Material

Name: CRFP

Description:

Material Behaviors

Elastic

General

Mechanical

Thermal

Electrical/Magnetic

Other

Elastic

Type: Lamina

☐ Use temperature-dependent data

Number of field variables: 0

Moduli time scale (for viscoelasticity): Long-term

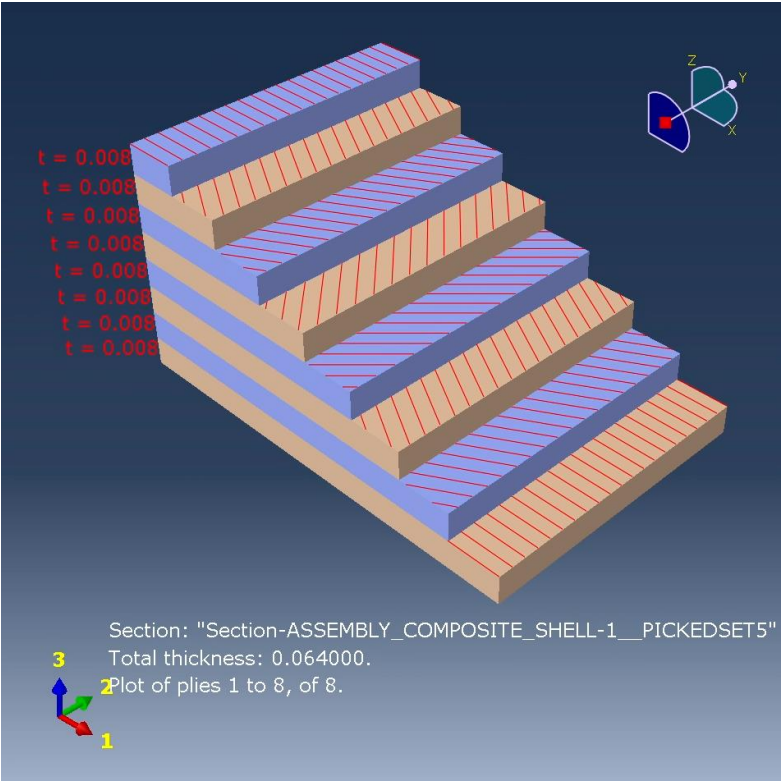
☐ No compression

☐ No tension

|   | E1   | E2   | Nu12 | G12   | G13   | G23   |
|---|------|------|------|-------|-------|-------|
| 1 | 12e6 | 12e6 | 0.05 | 0.7e6 | 0.5e6 | 0.5e6 |

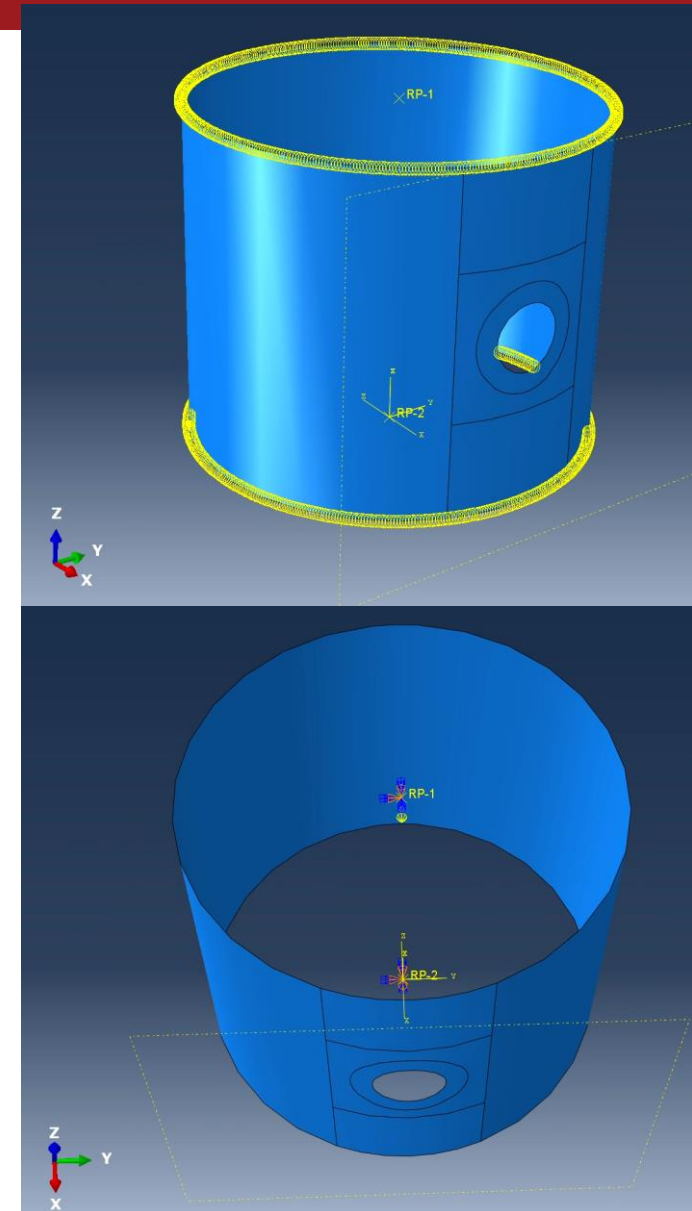
OK

Cancel



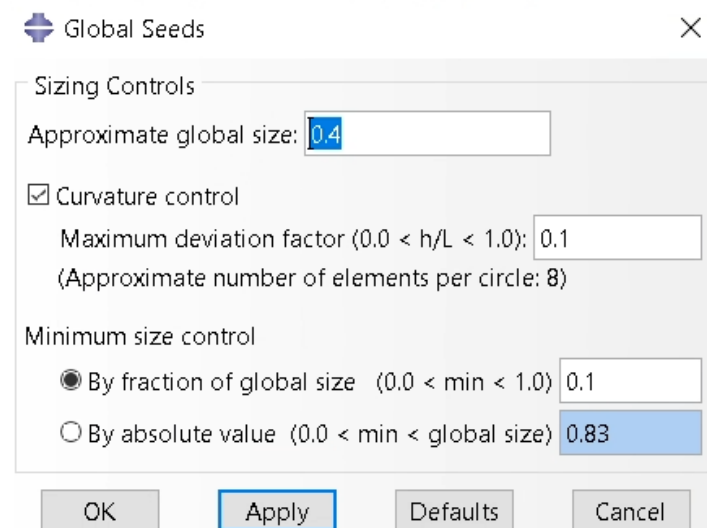
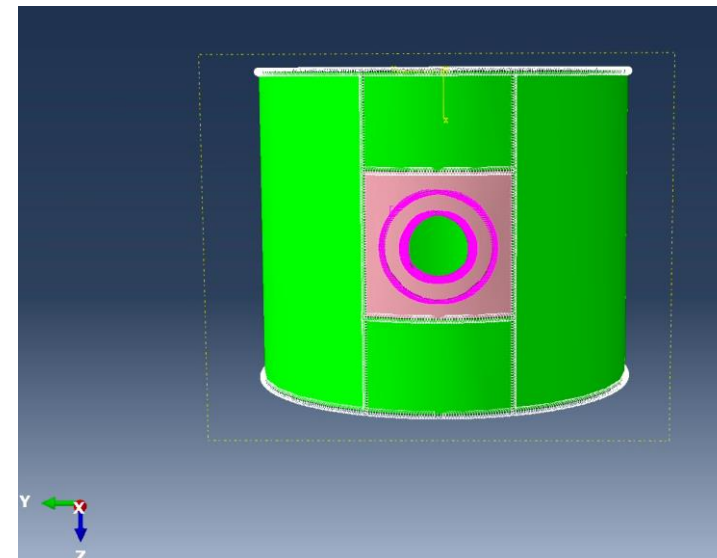
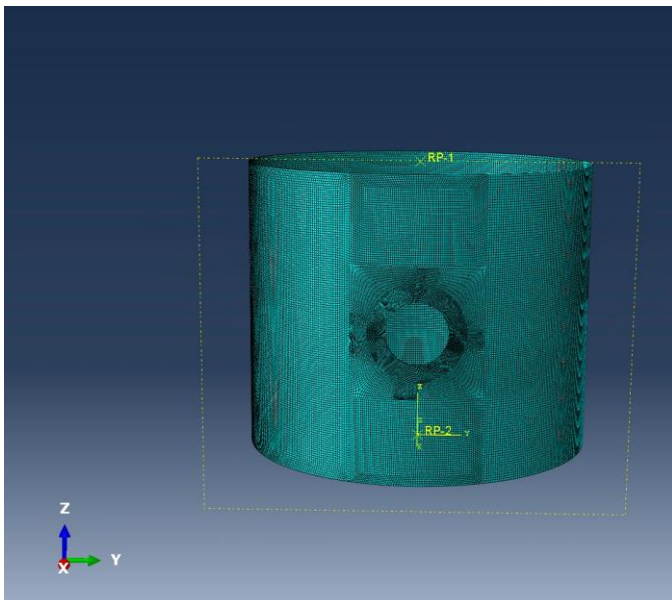
- **Boundary conditions and load**

- The top and bottom edges are rigid bodies
  - Sets are made to represent the edges (easier to select)
- Datum system is set to the bottom of the cylinder
- Reference points for top (RP-1) and bottom (RP-2) are set
- Boundary conditions
  - Bottom = fixed (Encastre)
  - Top = allows for displacement and rotation but, we only move in the cylinder axis (z-direction)
  - From problem statement, assuming clamped-clamped
  - Select everything except U3 (z-direction), only allowing axial movement
- Load
  - Applied at top using RP-1
  - CF3 = z-direction, + and – follow axis directing as shown
  - Because compression, CF3 = -1
    - The load points into the cylinder (compression)
- -1 is arbitrary number to get eigenvalue (critical load)



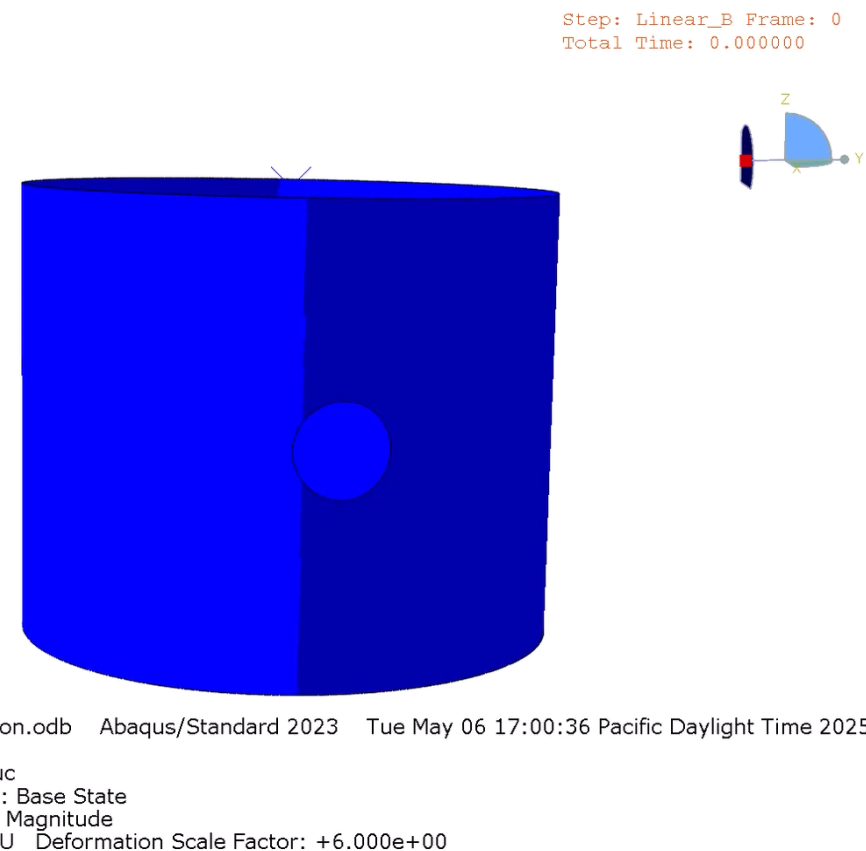
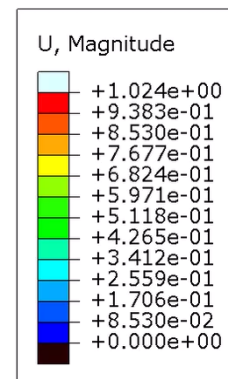
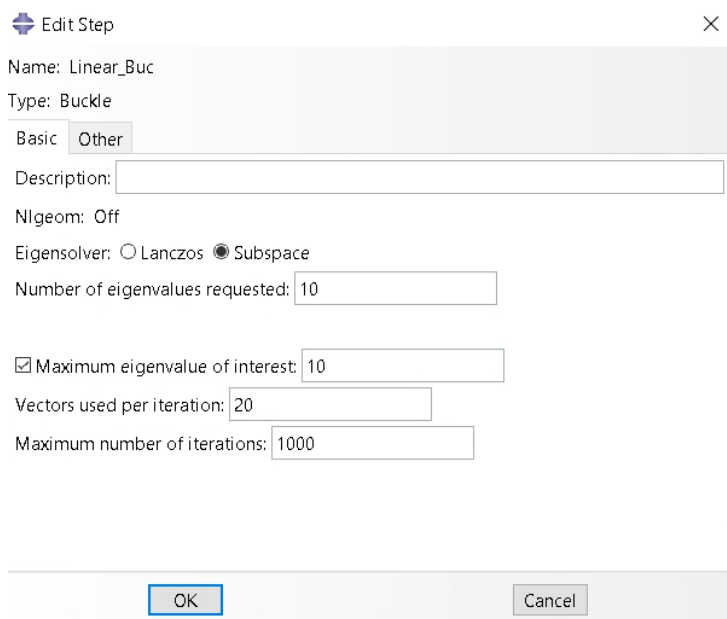
## • Mesh

- Elements is set as S4 by turning off reduced integration
- Majority of the cylinder (green) is set to “Structured” – makes mesh more reasonable
- Hole and close surrounding area within the partition lines are set to “Free” with medial axis turned on – makes it more symmetric
- Global seed is set to 0.4 – shown in the image
- The two circles are meshed independently to make it finer, local seeds are set “by number” and set to 300 element numbers



## Results

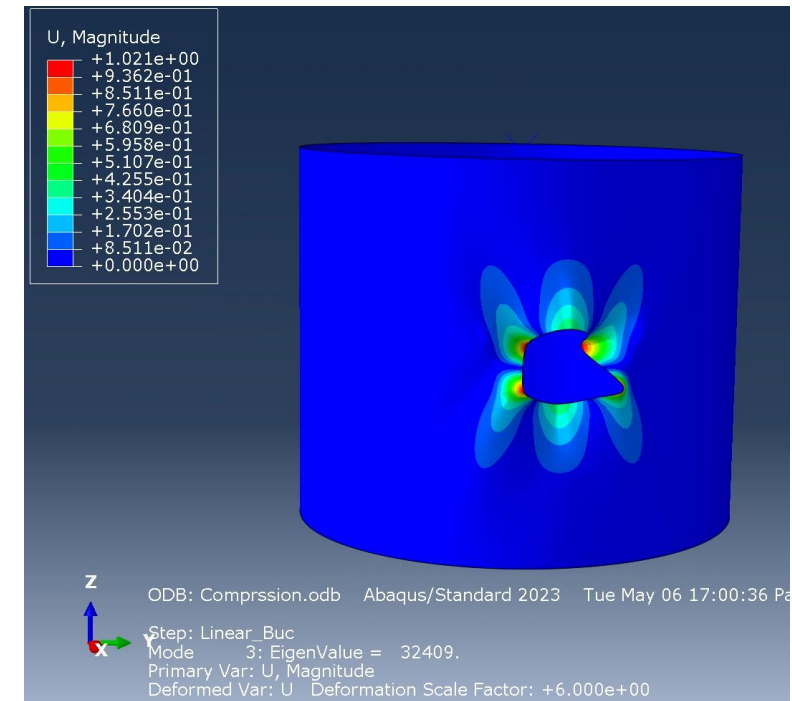
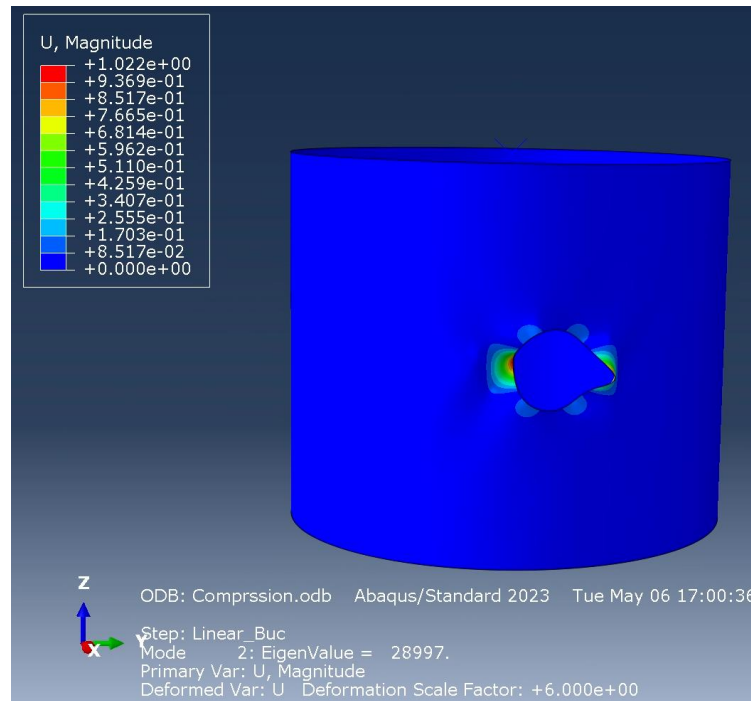
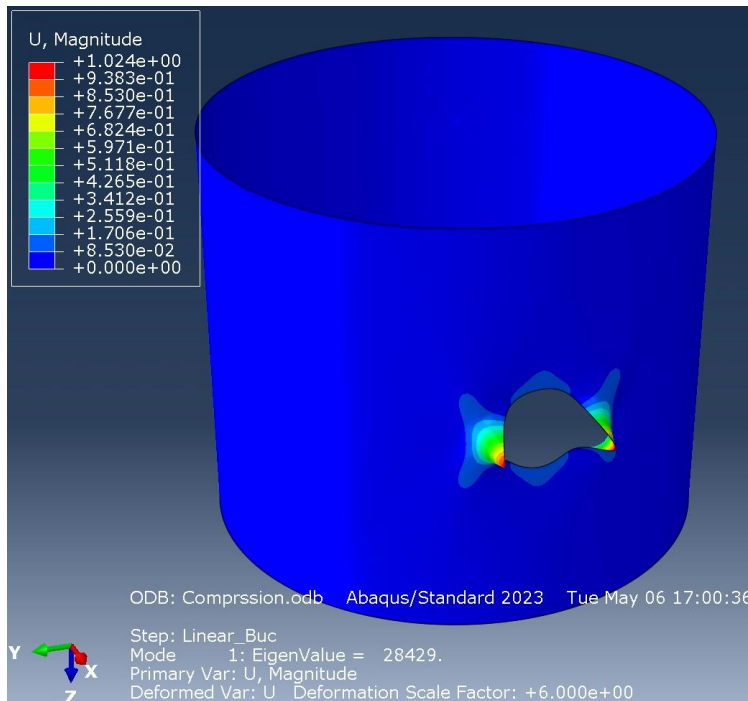
- Linear perturbation “Buckle” step is selected
- “Subspace” eigen solver is appropriate for smaller models
- We want 10 buckling modes (eigenvalues)
  - Only the first mode is relevant
- Set maximum number of iterations to about twice the number of eigenvalues
- GIF video of all eigenvalues/buckling modes (PRESS PLAY) →



Play button

## Linear model results

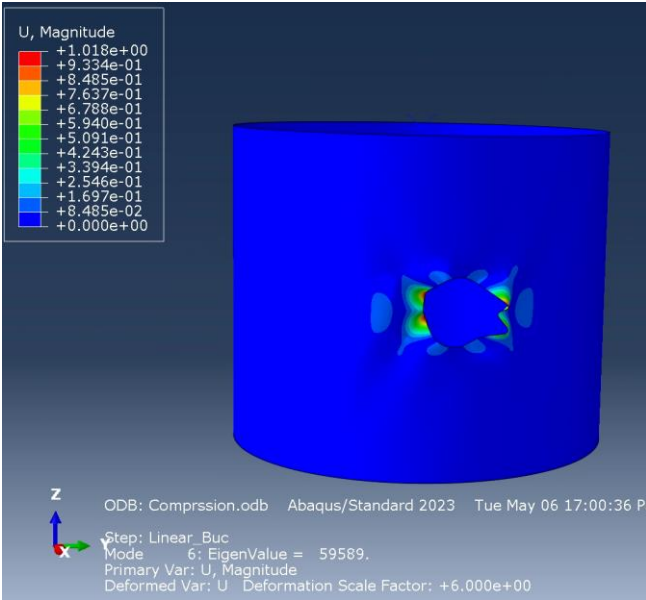
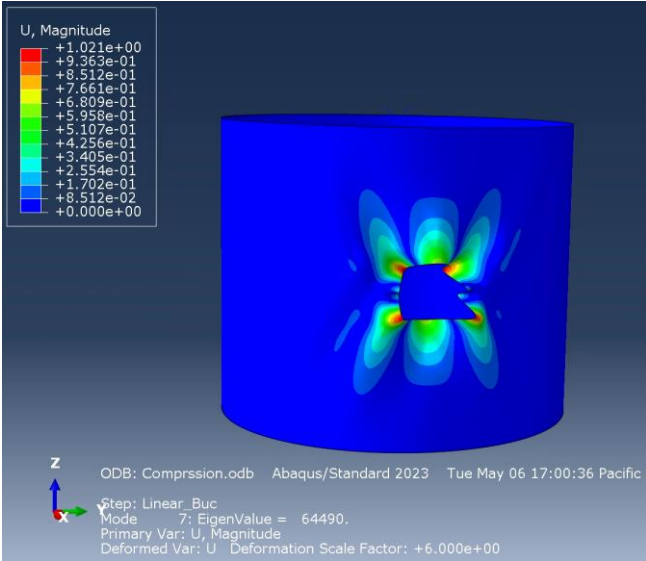
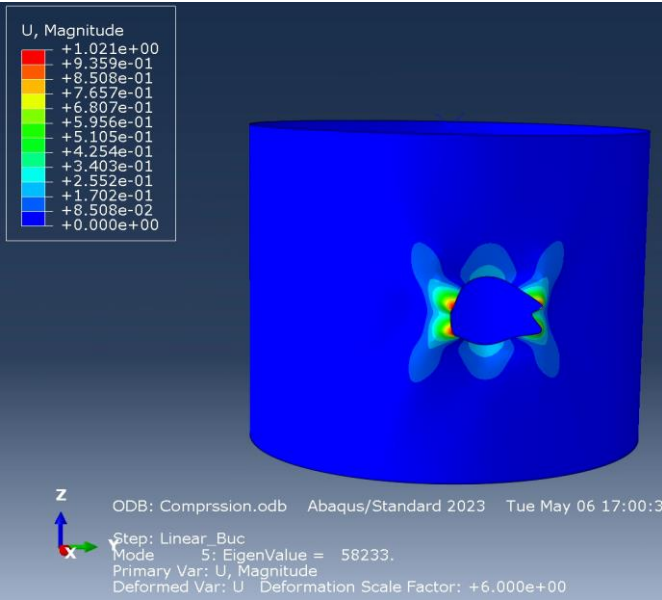
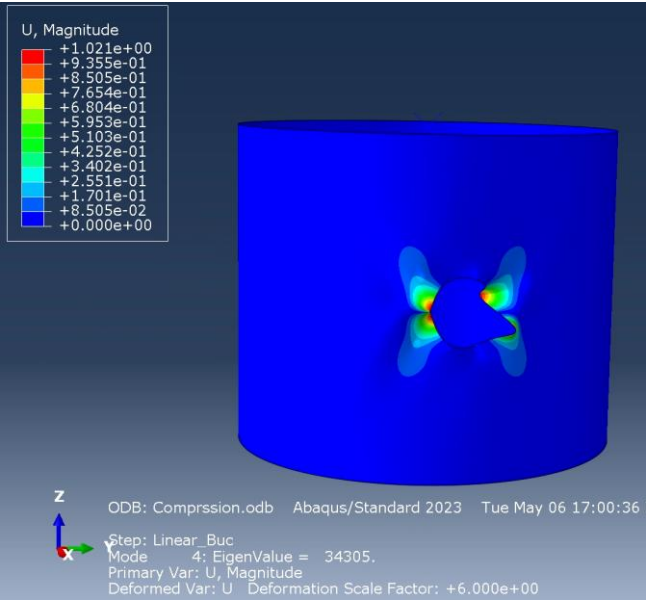
- Eigenvalues (First 3 modes)
  - 28429, 28997, 32409
  - Our reference load was -1, so we can use these values as the critical load when the shell buckles
- Knockdown factor = 0.5
- Minimum load where buckling observed (Mode 1) = 28429 lb.
- Compression design load allowable =  $0.5 * 28429 = 14214.5 \text{ lb.}$
- Mode shape of the buckle is shown in the image (leftmost image below = mode 1)
  - Mode 1 is the lowest eigenvalue which is the most critical failure mode
- Mode 2 and Mode 3 results are just shown for context
- Mode 1 is the most important



- Results

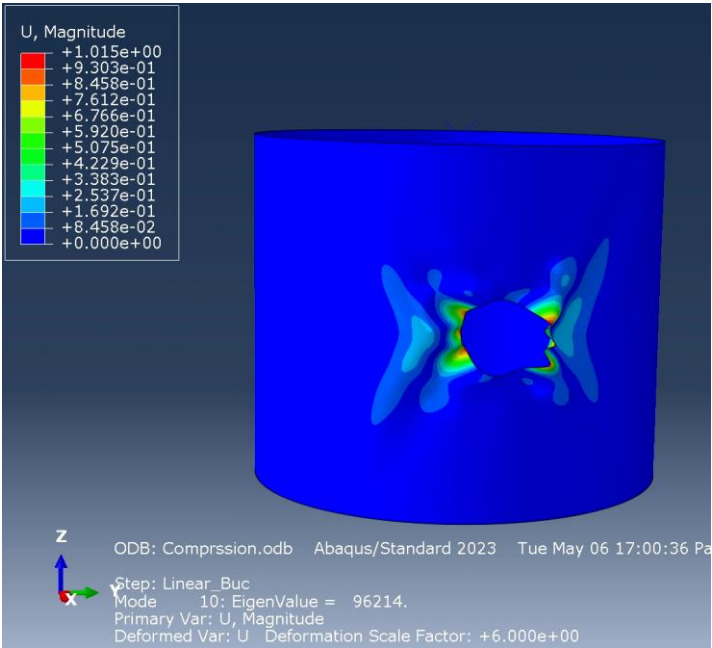
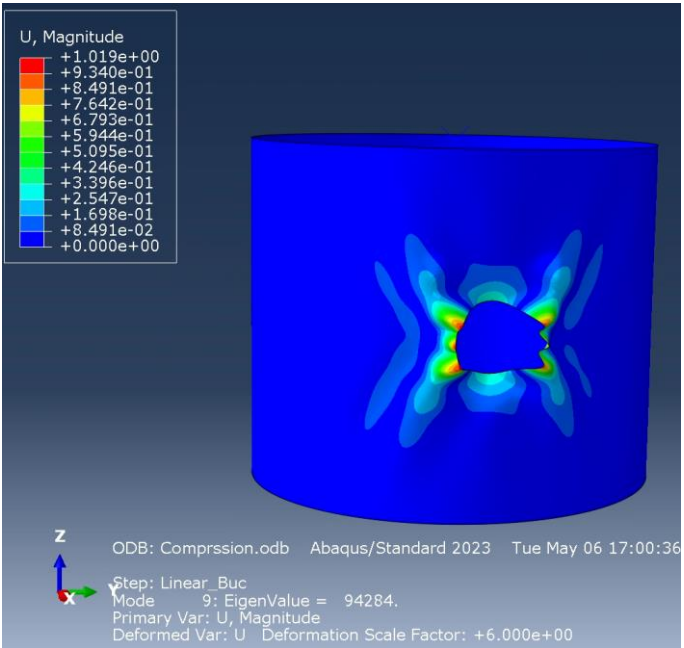
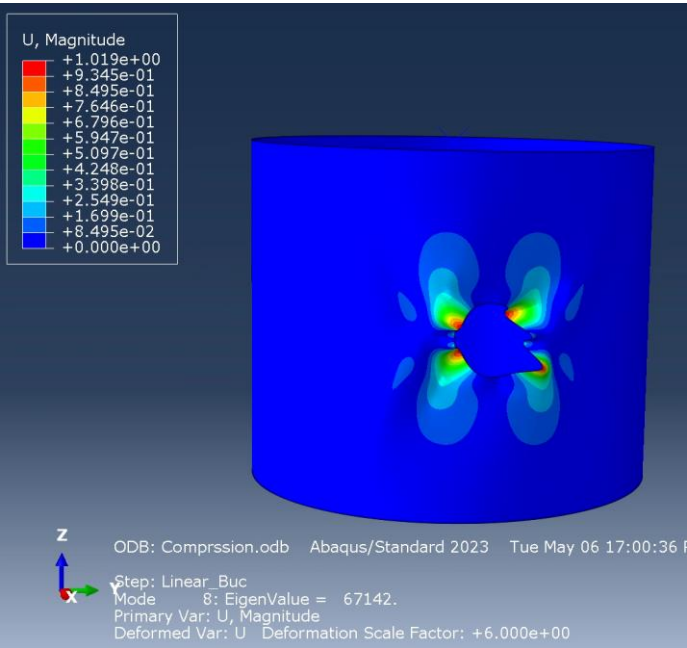
• Modes 4,5,6,7

• Just shown for context to show I did FEA correctly



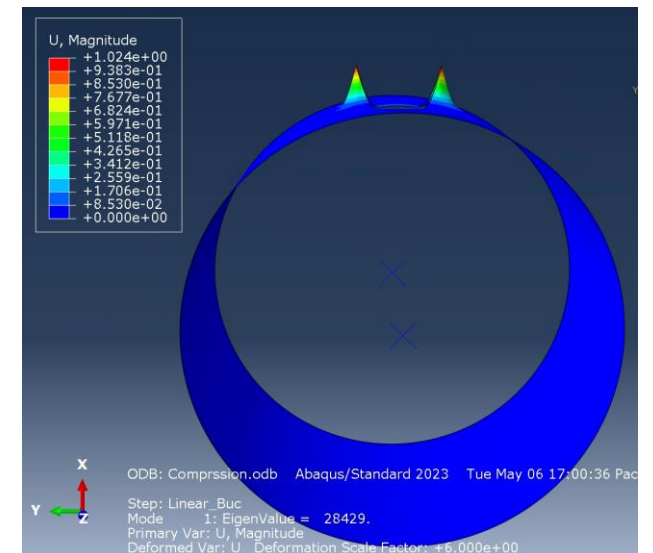
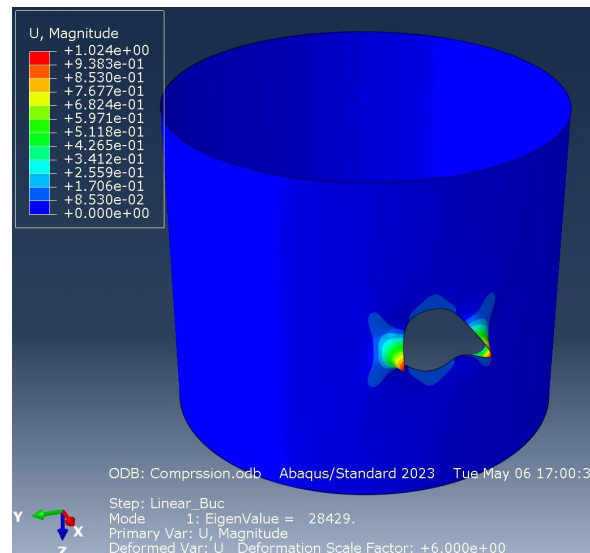
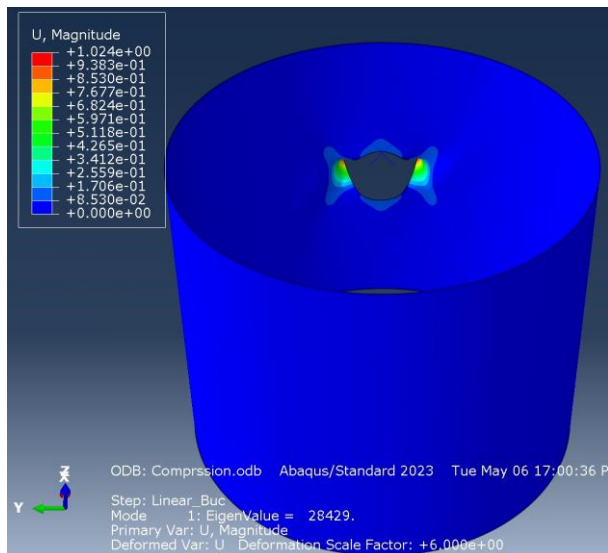
- Results

  - Modes 8, 9, 10
  - Just shown for context to show I did FEA correctly



## • Conclusion

- No nonlinear analysis was required for this Bonus Project but from 585 experience, we do know it is more accurate/less conservative for buckling modeling
  - The linear model underpredicts buckling capabilities
- Composite cylinder shells buckle differently than metal structures with cutouts
  - Buckling response is dominated by nonlinear effects
- To determine structure buckling loads, it is ideal to run physical testing and compare those results to analytical buckling loads found in FEA
- In Mode 1, our minimum load where buckling was observed = 28429 lb.
- Compression design load allowable accounting for knockdown factor
  - $= 0.5 * 28429 = 14214.5 \text{ lb.}$
- Mode shape of the buckling shown below in images (Mode 1)



## • Setup Changes

- Same setup as Question 1 for modeling
- Only thing that changes is laminate stacking sequence and new core material properties
- Core material properties are inputted
  - $E_{11} = 1$  ksi
  - $E_{22} = 1$  ksi
  - $\nu_{12} = 0.01$
  - $G_{12} = 0.6$  ksi
  - $G_{13} = 20$  ksi
  - $G_{23} = 20$  ksi
- Plys are changed to match new stacking sequence
  - $[0 / +45 / -45 / 0 / \text{Core} / 0 / +45 / -45 / 0]$
  - Core = 0 degrees
  - Not symmetric
- Started with 0.008 in. thick core to establish baseline test results
  - Thickness of core was iterated from here

Edit Material

Name: Core

Description:

Material Behaviors

Elastic

General Mechanical Thermal Electrical/Magnetic Other

Elastic

Type: Lamina

Use temperature-dependent data

Number of field variables: 0

Moduli time scale (for viscoelasticity): Long-term

No compression

No tension

Data

|   | E1  | E2  | ν12  | G12   | G13  | G23  |
|---|-----|-----|------|-------|------|------|
| 1 | 1e3 | 1e3 | 0.01 | 0.6e3 | 20e3 | 20e3 |

OK Cancel

Edit Section

Name: CFRP\_Sec

Type: Shell / Continuum Shell, Composite

Section integration: ☒ During analysis ☐ Before analysis

Layup name:

Basic Advanced

Thickness integration rule: ☒ Simpson ☐ Gauss

☐ Symmetric layers

| Material | Thickness | Orientation Angle | Integration Points |
|----------|-----------|-------------------|--------------------|
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| Core     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |

Options:

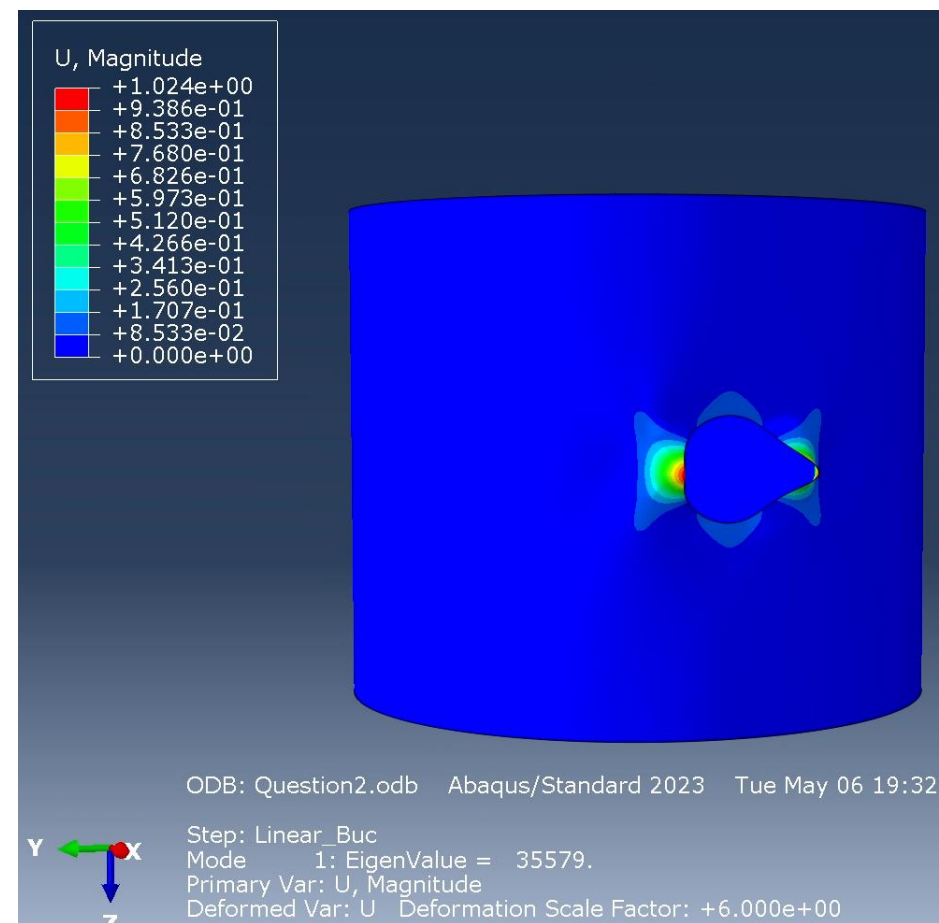
OK Cancel

## • Problem statement

- Problem statement says we need to determine core thickness to survive a max compression load of 2,000,000 lbs.
- Need to incorporate a knockdown factor for material imperfection and a F.O.S.
  - Knockdown = 0.5
  - F.O.S = 1.4 for human spaceflight
- We need the buckling loads to exceed:
  - $(20000000) \times (1.4) / (0.5) = 5,600,000 \text{ lbs.}$
- So, buckling load in the FEA needs to exceed 5,600,000 lbs. while still being as light as possible
- Mode 1 is the lowest eigenvalue which is the most critical failure mode (looking at these values)

## • First Run

- First trial was with 0.008 in. core thickness
- Mode 1 Eigenvalue = 35,579 lbs.
- Far too low, but good test for a baseline



- Second Run**
  - Core thickness set to 0.8 in.
  - Mode 1 Eigenvalue = 1,165,310 lbs.
  - Still buckling load was still too little but, getting close to value

Edit Section

Name: CFRP\_Sec
 

Type: Shell / Continuum Shell, Composite

Section integration:
 ☒ During analysis
 ☐ Before analysis

Layup name:

Basic

Advanced

Thickness integration rule:
 ☒ Simpson
 ☐ Gauss

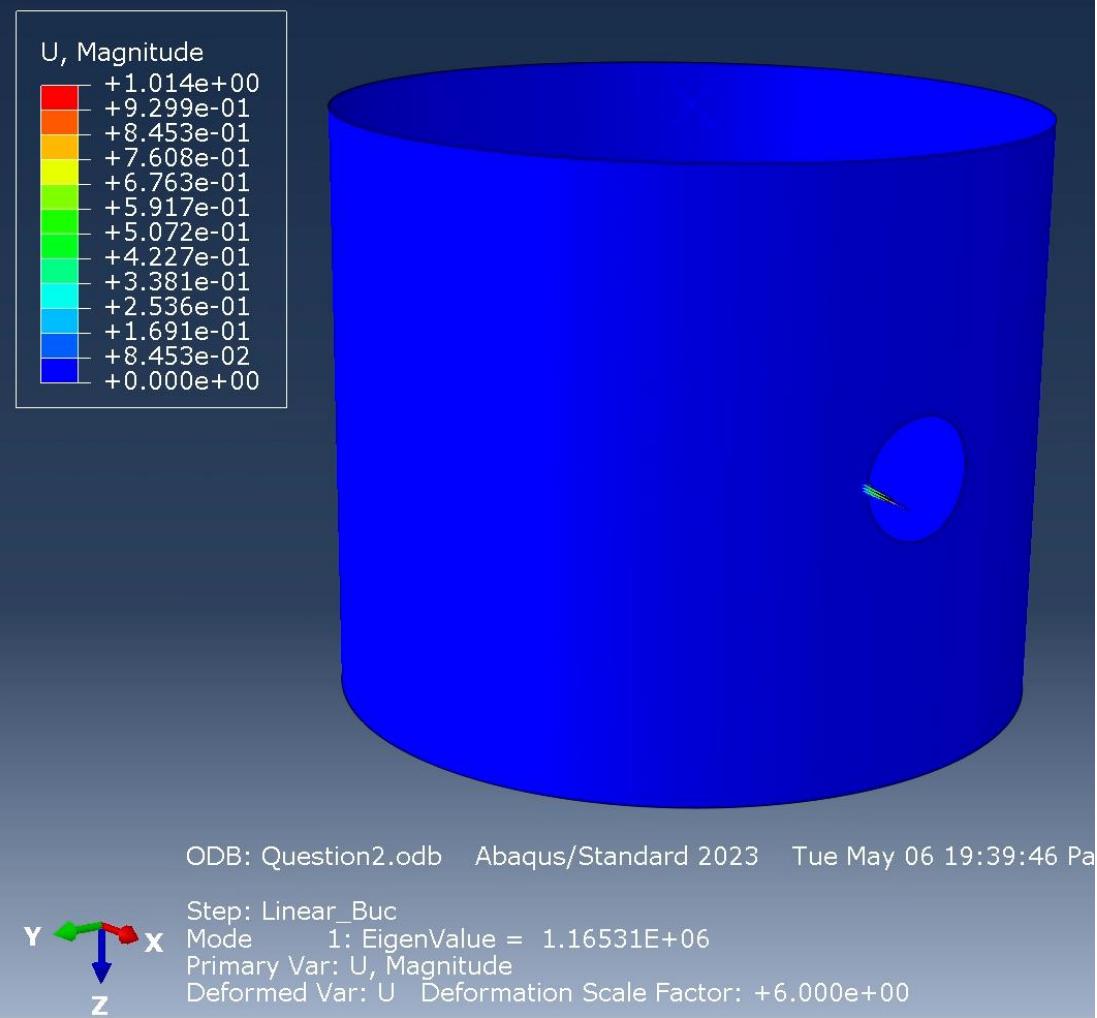
☐ Symmetric layers

| Material | Thickness | Orientation Angle | Integration Points |
|----------|-----------|-------------------|--------------------|
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| Core     | 0.8       | 0                 | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |

Options: 

OK

Cal



## • Third Run

- Core thickness set to 4 in.
- Mode 1 Eigenvalue = 5,780,140 lbs.
- Buckling load is greater than our expected load when including knockdown factor and F.O.S
  - $5,780,140 > 5,600,000$  lbs.
- We can do more iterations; we want the lightest available core, and we can slightly reduce the core thickness to achieve that

Edit Section

Name: CFRP\_Sec

Type: Shell / Continuum Shell, Composite

Section integration: ☒ During analysis ☐ Before analysis

Layup name:

Basic **Advanced**

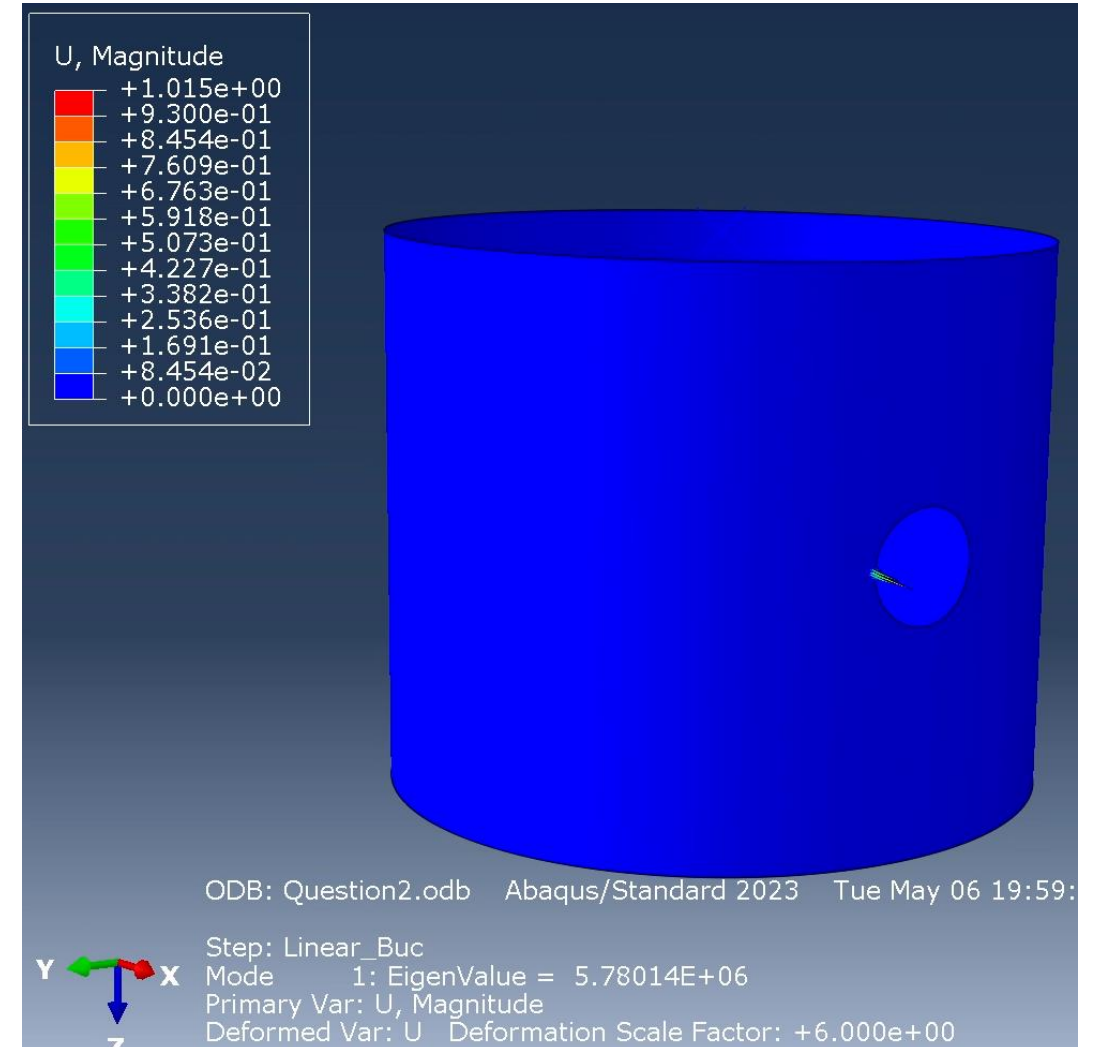
Thickness integration rule: ☒ Simpson ☐ Gauss

☐ Symmetric layers

| Material | Thickness | Orientation Angle | Integration Points |
|----------|-----------|-------------------|--------------------|
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| Core     | 4         | 0                 | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |
| CRFP     | 0.008     | 45                | 3                  |
| CRFP     | 0.008     | -45               | 3                  |
| CRFP     | 0.008     | 0                 | 3                  |

Options:

OK Car



- Last Run

  - Core thickness set to 3.9 in.
  - Mode 1 Eigenvalue = 5,632,670 lbs.
  - Buckling load was greater than our expected load when including knockdown factor and F.O.S

    - $5,632,670 > 5,600,000$  lbs.
  - This eigenvalue is perfect, we keep the weight of the core as light as possible and still exceed our necessary load requirements

Edit Section

Name: CFRP\_Sec

Type: Shell / Continuum Shell, Composite

Section integration:

☒ During analysis

☐ Before analysis

Layup name:

Basic

Advanced

Thickness integration rule:

☒ Simpson

☐ Gauss

☐ Symmetric layers

| Material | Thickness | Orientation Angle |
|----------|-----------|-------------------|
| CRFP     | 0.008     | 0                 |
| CRFP     | 0.008     | 45                |
| CRFP     | 0.008     | -45               |
| CRFP     | 0.008     | 0                 |
| Core     | 3.9       | 0                 |
| CRFP     | 0.008     | 0                 |
| CRFP     | 0.008     | 45                |
| CRFP     | 0.008     | -45               |
| CRFP     | 0.008     | 0                 |

U, Magnitude

+1.015e+00

+9.300e-01

+8.454e-01

+7.609e-01

+6.763e-01

+5.918e-01

+5.073e-01

+4.227e-01

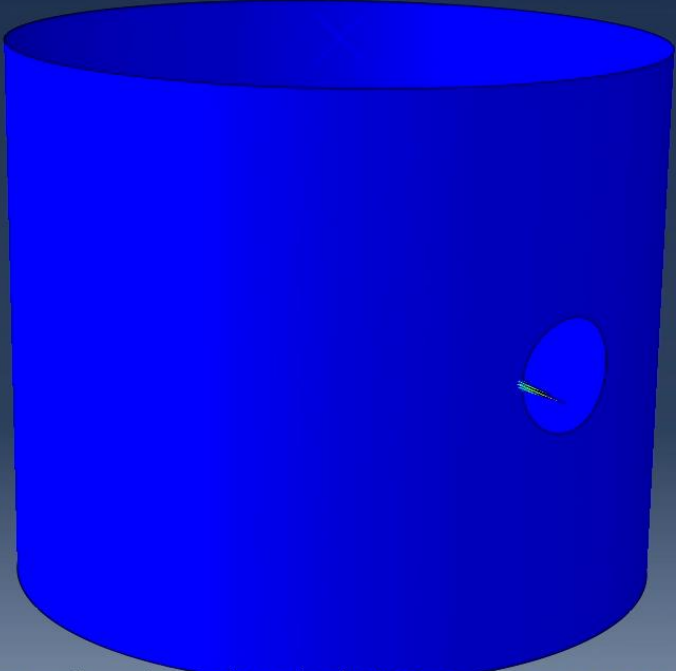
+3.382e-01

+2.536e-01

+1.691e-01

+8.454e-02

+0.000e+00



ODB: Question2.odb

Abaqus/Standard 2023

Tue May 06 20:14:16

Step: Linear\_Buc

Mode 1: EigenValue = 5.63267E+06

Primary Var: U, Magnitude

Deformed Var: U Deformation Scale Factor: +6.000e+00

Y

X

Z

- **Conclusion**

- The buckling load from linear buckling analysis with a 3.9 in. core thickness = 5,632,670 lbs.
  - No need to reduce more
- This is slightly greater than our required minimum buckling load (after applying knockdown and F.O.S)
- This minimizes weight of the core as much as possible, of course I could reduce the core thickness more by removing a 100<sup>th</sup> of an inch but, I deemed it was unnecessary and hard to manufacture in real life
- I also like the “pocket margin” with the 3.9-inch-thick core
- We also know that linear analysis errs very conservatively, so I am happy with a 3.9 in. core and even happier with a 4.0-inch core if weight requirements allow it
  - 4.0 in. is an easy even number that could be easier to manufacture in real application. (just a suggestion/commentary)
- The sandwich design of the core significantly improves buckling resistance with minimal weight penalty
- Thank you, Professor Goyal and Aniket!